

Introduction to the weighted projective lines

- (1) **Constructing weighted projective lines from canonical algebras.**
 - Rough structure of $\text{mod}(\Lambda)$ (Λ canonical), separating tubular family. ([7])
 - Sketch of tubular shifts [4, (S10)].
 - Construction of $\mathcal{H} = \text{coh}(\mathbb{X})$ in $D^b(\Lambda)$ and its properties ([4, Thm. 6.1]). (Hereditary, noetherian, ... with tilting object T such that $\text{End}(T) = \Lambda$.)
- (2) **Axiomatic approach to weighted projective lines.**
 - Starting with axioms (\mathcal{H} hereditary, noetherian, ... category with tilting object like in [6, Ch. 10], or [5]) show existence of tilting object T with $\text{End}(T)$ canonical and that $\mathcal{H} = \text{coh}(\mathbb{X})$ as in (1).
 - Review Happel's theorem classifying hereditary categories with tilting object up to derived equivalence. ([6, Thm 6.3].)
- (3) **Vector bundles and Cohen-Macaulay modules.**
 - The graded algebra $S(p, \lambda)$. ([2, Ch. 1].)
 - Serre's theorem [2, 1.8]. Avoiding sheaves one can sketch the (much more general) proof in [1, Thm. 4.5] (using [2, (1.5.5)]).
 - Correspondence between torsionfree objects (vector bundles) and CM-modules [2, Thm. 5.1], [3, 7.5+8.3].
- (4) **Representation type and Euler characteristic.** Stability (semistability, resp.) of indecomposable bundles in case of positive (zero, resp.) Euler characteristic. ([2, Ch. 5] and [6, Ch. 10].) Shape of the categories in case of positive, zero, negative Euler characteristic, resp.

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